

## The Laws of Logarithms: Products & Quotients & Powers & Roots

### † The Law of Logarithms with regard to Products and Quotients of Numbers \*

Many times students see no value in these type of problems, however, when confronted with an advanced problem where these laws apply they will.

The Log of a Product equal the Sum of the Logs \*  $\text{Log}(A) \times (B) = \text{Log}(A) + \text{Log}(B)$

$(.046) \times (7384) = N$	Determine the Product using Logs.
$(\text{Log}) (.046) \times (7384) = N$ (Log)	Take the Log of both Sides
$(\text{Log}) (.046) (\text{Log}) (7384) = \text{Log } N$	Distribute the Log on both sides
$\text{_____} + \text{_____} = \text{Log } N$	Determine Log of ( ) & ( ) then Add
$(\text{Anti}) \text{_____} = \text{Log } N$ (Anti)	Take the AntiLog of both sides
$\text{_____} = N$	Check N in $10^x = N$

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The Log of a Quotient equal the Difference of the Logs \*  $\text{Log}(A) \times (B) = \text{Log}(A) - \text{Log}(B)$

$(528) / (.073) = N$	Determine the Quotient using Logs.
$(\text{Log}) (528) / (.073) = N$ (Log)	Take the Log of both Sides
$(\text{Log}) (528) - (\text{Log}) (.073) = \text{Log } N$	Distribute the Log on both sides
$\text{_____} - \text{_____} = \text{Log } N$	Determine Log of ( ) & ( ) then Subtract
$(\text{Anti}) \text{_____} = \text{Log } N$ (Anti)	Take the AntiLog of both sides
$\text{_____} = N$	Check N in $10^x = N$

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Tom Love                      Malone College                      Fall 2003

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### † The Law of Common Logarithms with regard to Powers and Roots of Numbers \*

Many times students see no value in these type of problems, however, when confronted with an advanced problem where these laws apply they will.

The Log of a Power equal the Power X the Log of Number \*  $\text{Log}(A)^P = P \times \text{Log}(A)$

$(648)^7 = N$	Determine the Seventh Power of (648)
$(\text{Log}) (648)^7 = N$ (Log)	Take the Log of both Sides
$7 \times (\text{Log}) (648) = \text{Log } N$	Distribute the Log on both sides
$7 \times \text{_____} = \text{Log } N$	Determine Log of ( ) & Multiply by 7
$(\text{Anti}) \text{_____} = \text{Log } N$ (Anti)	Take the AntiLog of both sides
$\text{_____} = N$	Check N in $10^x = N$

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The Log of a Root equal the Root X the Log of Number \*  $\text{Log}(A)^R = R \times \text{Log}(A)$

$(.007)^{1/5} = N$	Determine the Fifth Root of (.007)
$(\text{Log}) (.007)^{1/5} = N$ (Log)	Take the Log of both Sides
$(1/5) \times (\text{Log}) (.007) = \text{Log } N$	Distribute the Log on both sides
$(1/5) \times \text{_____} = \text{Log } N$	Determine Log of ( ) & Multiply by (1/5)
$(\text{Anti}) \text{_____} = \text{Log } N$ (Anti)	Take the AntiLog of both sides
$\text{_____} = N$	Check N in $10^x = N$

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$7 \times \text{_____} = \text{Log } N$	Determine Log of ( ) & Multiply by 7
$(\text{Anti}) \text{_____} = \text{Log } N$ (Anti)	Take the AntiLog of both sides
$\text{_____} = N$	Check N in $10^x = N$

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The Log of a Root equal the Root X the Log of Number \*  $\text{Log}(A)^R = R \times \text{Log}(A)$

$(.007)^{1/5} = N$	Determine the Fifth Root of (.007)
$(\text{Log}) (.007)^{1/5} = N$ (Log)	Take the Log of both Sides
$(1/5) \times (\text{Log}) (.007) = \text{Log } N$	Distribute the Log on both sides
$(1/5) \times \text{_____} = \text{Log } N$	Determine Log of ( ) & Multiply by (1/5)
$(\text{Anti}) \text{_____} = \text{Log } N$ (Anti)	Take the AntiLog of both sides
$\text{_____} = N$	Check N in $10^x = N$

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